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# Speckle reduction in SAR Imagery by various multi-look techniques

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Speckle reduction in SAR Imagery by

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SAR beelden bevatten speckle, een type ruis dat ontstaat door de coherente verwerking van radar-echo's van gedistribueerde doelen. De aanwezigheid van deze ruis vermindert de detecteerbaarheid van objecten in het beeld. De mogelijkheid om gedistribueerde doelen te scheiden en te classificeren, vermindert eveneens. Zoals elke ruisvorm kan speckle worden gereduceerd door middelen, het samennemen van een aantal beeldrealisaties van dezelfde scene. Eén van de technieken die kan worden gebruikt is 'multi-look processing'. Hierbij worden de samenstellende beelden, de 'single-look' beelden, gevormd door voor elk beeld een deel van de beschikbare signaalbandbreedte te gebruiken. Elk deel wordt dan verwerkt tot een single-look beeld van dezelfde scene. Het ruisgereduceerde beeld, het multi-look beeld, wordt verkregen door de beelden incoherent, pixel voor pixel, op te tellen.

Het speckle-gereduceerde beeld heeft nu een verbeterde radiometrische resolutie. Echter, omdat de single-look beelden slechts een deel van de beschikbare bandbreedte gebruiken, zal de geometrische resolutie slechter zijn. De verbeterde radiometrische resolutie wordt verkregen ten koste van de geometrische resolutie. De resulterende resoluties worden bepaald door de manier waarop de beschikbare bandbreedte wordt verdeeld en de gebruikte weegfunctie. Het toepassen van weegfuncties verbetert het zijlusgedrag van de corresponderende impulsresponsie, de lekkage, het zich uiten van (sterke) reflecties buiten de doelpositie wordt dan minder. Dit verbeterde 'lekkage' gedrag gaat ten koste van de geometrische resolutie, dat wil zeggen de breedte van de hoofdlus van de puntdoelresponsie neemt toe.

In dit rapport worden een aantal multi-look technieken onderzocht, die zich onderscheiden in de vorm van de weegfunctie, de breedte van de weegfunctie, de combinatie van verschillende weegfuncties en de posities van de weegfuncties ten opzichte van elkaar.

De voor het beoordelen van de technieken benodigde maten worden behandeld. Deze maten zijn: het equivalente aantal beelden, ENL, hetgeen een maat is voor de ruisvermindering, en de vermogenshalfwaardebreedte van de hoofdlus van de puntdoelresponsie, zijnde een maat voor de geometrische resolutie.

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#### 1. Introduction

Speckle appears in SAR images due to coherent processing of radar echoes of distributed target scatterers. Its presence in SAR images reduces the detectability of objects in the image and also the capability to separate and classify distributed targets. Noise can be reduced by averaging. One technique which can be used is multi-look processing. Here the available signal bandwidth is divided in L parts. Each part is processed yielding a single look image of the same scene. By adding the looks incoherently pixel by pixel the speckle reduced image is obtained. The speckle reduced image has an improved radiometric resolution. However, since the single look images use only part of the available bandwidth, the geometric resolution will be worse. Improvement of the radiometric resolution is obtained at the cost of the geometric resolution. The resulting resolutions are determined by: how the available bandwidth is partioned and the weighting function used. Using a weighting function improves the sidelobe behaviour of the corresponding impulse response at the expense of a broadening of the main lobe and thus a degradation of the geometric resolution, see [3]. In section 2 we introduce the improvement factor ENL, the Equivalent Number of Looks. The various multi-looking techniques are treated in section 3.

# 2. The improvement factor ENL, the Equivalent Number of Looks

The SAR image of an area of distributed targets will show speckle noise. The observed <u>intensity</u> from a pixel follows exponential statistics. The exponential distribution of a single look intensity image is given by

$$p(I) = \frac{1}{2\sigma^2} e^{\frac{-I}{2\sigma^2}}$$

where the mean value

$$m_{\rm I}=E[{\rm I}]=2\sigma^2$$

and the standard deviation is equal to this mean value

$$\sigma_{\rm I} = {\rm E} \Big[ \Big( {\rm I} - \overline{\rm I} \Big)^2 \Big] = 2 \sigma^2$$

In the sequel we assume an available processing bandwidth of  $B_a$  with corresponding available azimuth integration time  $T_a$ .

We further assume a flat azimuth SAR spectrum, see Figure 1. In practice this assumption is not valid since the azimuth spectrum is shaped by the azimuth antenna gain. In satellite SAR the available bandwidth  $B_a$  is roughly 0.8 PRF and the edges of the spectral interval coincide with the 3-dB points of the azimuth beam. We also assume that the thermal noise is small compared to the clutter.

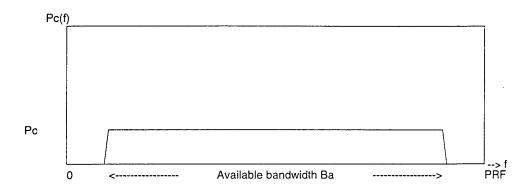


Figure 1: The azimuth SAR spectrum.

The noise behaviour of single look images is the same, irrespective of their geometric resolution and their spectral position in the available bandwidth (flat spectrum assumption!). To show this, let the mean intensity value of look 1 be  $m_1$  and the variance  $var_1$  and the corresponding values of look 2  $m_2$  and  $var_2$ , then by a simple scaling we can obtain a scaled image with the mean value  $m_1$ .

$$m_2' = km_2 = m_1$$

where k is the scaling constant. For the variance of the scaled image we find

$$var_2' = k^2 var_2$$

with  $var_2 = m_2^2$  we have

$$var_2' = k^2 m_2^2 = m_1^2 = var_1$$

Thus the scaled image has the same mean value and variance as the look 1 image.

We now compare the variances of a multi-look image with  $m_2$  and  $var_2$  composed of single look images with  $m_1$  and  $var_1$ . The multi-look image is formed so that  $m_2 = m_1$ . We define the equivalent number of looks (ENL) by

$$var_2 = \frac{1}{ENL} var_1$$

Thus ENL = 
$$\frac{\text{var}_1}{\text{var}_2} = \frac{\text{m}_1^2}{\text{var}_2} = \frac{\text{m}_2^2}{\text{var}_2}$$

The ENL corresponds to the effective number of statistically independent looks and is given by

$$ENL = \frac{E[I_M]^2}{var[I_M]}$$

where I<sub>M</sub> is the intensity of the multi-look image.

In the next chapter we discuss several multi-look techniques where a multi-look intensity image is a weighted sum of single look intensity images.

## 3. Multi-look techniques

#### 3.1 Rectangular weighting function, equal looks

The rectangular weighting function is given by

$$w(t) = 1 -T/2 \le t \le T/2$$

Figure 2 shows the weighting function and the corresponding azimuth impulse response profile  $g(t_a)$ .

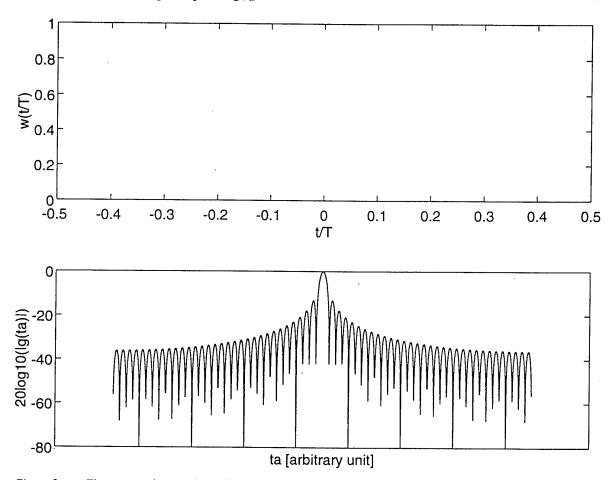


Figure 2: The rectangular weighting function and the corresponding azimuth impulse response profile.

#### 3.1.1 Full resolution image

The full resolution image uses the whole available bandwidth and no weighting function. So the best geometric resolution is obtained. Using the 3-dB resolution measure, the 3-dB bandwidth of the azimuth impulse response is  $0.81/B_a$ , where  $B_a$  is the available bandwidth.

Since no geometrical resolution is sacrificed, no speckle reduction is obtained.

$$ENL = \frac{E[I]}{var[I]} = 1$$

#### 3.1.2 Combination of L<sub>i</sub> independent looks

The available integration time is divided into  $L_i$  discrete contiguous segments. Each segment is used to generate a lower resolution single look image. The width of each segment is thus  $T=\frac{T_a}{L_i}$ . The geometrical resolution is reduced by a factor

 $L_i$ . Thus the 3-dB bandwidth of the azimuth impulse response is  $\frac{0.81L_i}{B_a}$ .

The mean values and (cross-)variances of the look images are given by  $\bar{I}_1 = \bar{I}$  for each look image 1.

$$\overline{(I_i - \overline{I}_i)(I_j - \overline{I}_j)}$$
 = var I for j = i and  
= 0 for j \neq i (independent looks!)

The multi-look intensity is given by

$$I_M = \alpha \sum_{i=1}^{L_i} I_i$$

The mean value  $\, \overline{I}_M = \alpha \sum_{i=1}^{L_i} \overline{I}_I = \alpha L_i I \, .$ 

The mean value is chosen equal to the single look's mean value, so

$$\alpha L_i = 1$$

The variance follows from

$$\overline{\left(I_{M} - \overline{I}_{M}\right)^{2}} = \alpha^{2} \overline{\left(\sum_{l=1}^{L_{i}} \left(I_{l} - \overline{I}_{l}\right)\right)^{2}} = \alpha^{2} L_{i} \operatorname{var}(I)$$

Hence

$$var I_{M} = \frac{var(I)}{L_{i}}$$

Thus the equivalent number of looks is

$$ENL = \frac{\bar{I}_{M}^{2}}{varI_{M}} = L_{i}$$

Hence the equivalent number of looks is equal to the number of independent looks.

#### 3.1.3 Combination of L overlapping looks

The available integration time is divided into L overlapping segments. The width of each segment corresponds to one of the L<sub>i</sub> looks in the independent case (see

3.1.2),  $T = T_a/L_i$ . The L single-look images are incoherently averaged. The mean values and the (cross-)variances of the look images are given by

 $\bar{\mathbf{I}}_1 = \bar{\mathbf{I}}$  for each look image 1.

$$var(I_1) = \overline{(I_1 - \overline{I}_1)^2} = \sigma_1^2 = \sigma^2 \text{ var } I \text{ for each look image } I$$

$$\overline{\left(I_{i}-\overline{I}_{i}\right)\left(I_{j}-\overline{I}_{j}\right)}=\rho_{ij}\sigma_{i}\sigma_{j}=\rho_{ij} \text{ var } I$$

where  $\rho_{ij}$  is the correlation coefficient between the i-th and j-th look image. The correlation coefficient  $\rho_{ij}$  depends on the degree of overlap. Since all looks have equal weighting,  $0 \le \rho_{ij} \le 1(\rho_{ij} = 1$ , complete overlap and  $\rho_{ij} = 0$ , complete separation). In appendix A the formula for the correlation coefficient is derived. Figure 3 shows the correlation coefficient as a function of the fractional overlap. As is shown in the appendix, the correlation coefficient  $\rho_{ij} = \rho_{I_iI_j}$  between the intensity images is equal to  $\left|\rho_{x_ix_j}\right|^2$ , where  $\rho_{x_ix_j}$  is the correlation coefficient between the complex valued images  $x_i$  and  $x_j$ . The multi-look intensity is given by

$$I_{M} = \alpha \sum_{i=1}^{L} I_{i}$$

Proceeding as before we arrive at

$$\bar{I}_M = \bar{I} \implies \alpha = \frac{1}{L}$$

$$var(I_M) = \frac{\sum_{i=1}^{L} \sum_{j=1}^{L} \rho_{ij}}{L^2} var I$$

Thus

$$ENL = \frac{L^2}{\sum_{i=1}^{L} \sum_{j=1}^{L} \rho_{ij}}$$

It turns out that an increase of the ENL is possible, see figure 4. Since the width of the looks is the same as in case 3.1.2, the geometric resolution is the same.

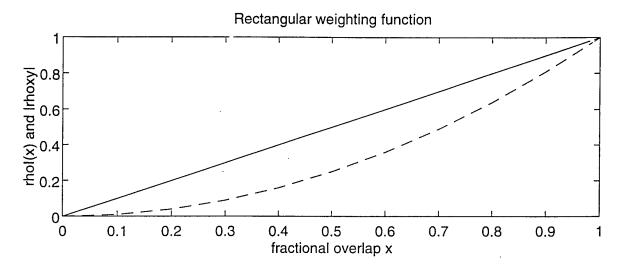


Figure 3: The correlation coefficient as a function of the fractional overlap complex images  $|\rho_{xy}(x)|$  intensity images  $\rho_1(x)$ 

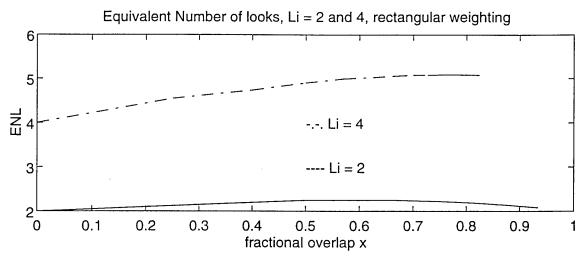


Figure 4: The ENL as a function of the fractional overlap.

#### 3.2 Hamming weighting function, equal looks

The Hamming window is a frequently used one (see 3). The function is given by

$$w(t) = \alpha + (1 - \alpha)\cos\left(\frac{2\pi}{T}t\right) - T/2 \le t \le T/2$$

with  $\alpha = 0.54$ .

The 3-dB bandwidth of the azimuth impulse response profile is 1.30/B<sub>a</sub>.

Figure 5 shows the weighting function and the corresponding azimuth impulse response profile  $g(t_a)$ .

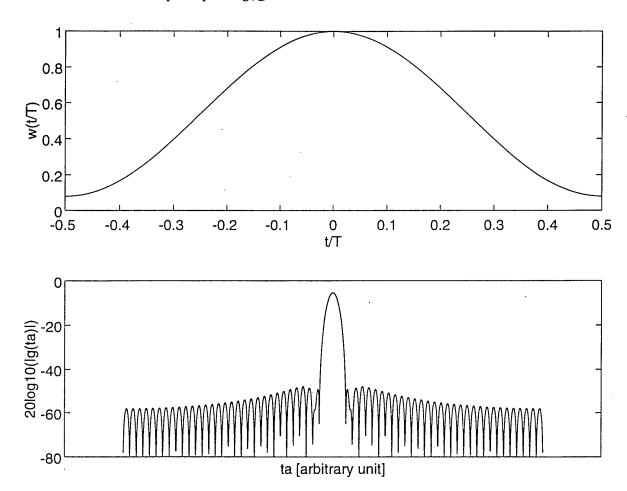


Figure 5: The Hamming weighting function and the corresponding azimuth impulse response profile.

#### 3.2.1 Combination of L<sub>i</sub> independent looks

Proceeding as in 3.1.2 we find

The multi-look intensity image is  $I_M = \frac{1}{L_i} \sum_{l=1}^{L_i} I_l$ , the mean value,  $\bar{I}_m = \bar{I}$  and the

variance, 
$$var(I_M) = \frac{var(I)}{L_i}$$
, thus the ENL =  $L_i$ .

Comparing this case, the Hamming window, with the results from 3.1.2, the rectangular window, we see that the speckle reduction is the same. However, the geometric resolution is now worse. So, we expect that with Hamming windows a better speckle reduction is attainable. The technique discussed next shows that this is indeed possible.

#### 3.2.2 Combination of L overlapping looks

Proceeding as in 3.1.3 we find The multi-look intensity image is

$$I_{M} = \frac{1}{L} \sum_{l=1}^{L} I_{l}$$

the mean value  $\bar{I}_M = \bar{I}$ 

the variance 
$$var(I_M) = \frac{\sum_{i=1}^{L} \sum_{j=1}^{L} \rho_{ij} var I}{L^2}$$

the Equivalent Number of Looks is ENL = 
$$\frac{L^2}{\sum_{i=1}^{L}\sum_{j=1}^{L}\rho_{ij}}$$

Figure 6 shows the correlation coefficient as a function of the fractional overlap.

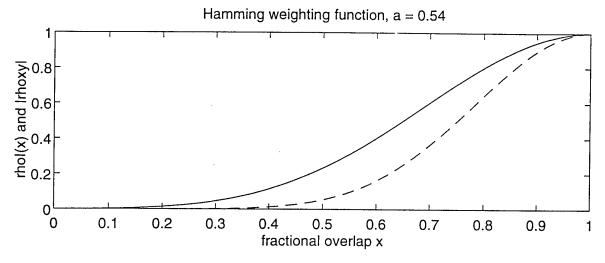


Figure 6: The correlation coefficient as a function of the fractional overlap: complex images  $|\rho_{xy}(x)| = \frac{1}{1-\frac{1}{2}}$  intensity images  $|\rho_{I}(x)| = \frac{1}{1-\frac{1}{2}}$ 

As derived in appendix A,  $\rho_{ij} = \rho_{I_iI_j} = \left| \rho_{x_ix_j} \right|^2$ , where  $\rho_{I_iI_j}$  is the correlation coefficient of the intensity images and  $\rho_{x_ix_j}$  is the correlation coefficient of the complex images.

Comparing the  $\rho$ -values from this figure with those of figure 3, we see that the 'Hamming' values are smaller. This means that with the same value of the sum of the correlation values we can have more looks in the Hamming case, thus an increased ENL.

Figure 7 shows the ENL as a function of the (overlapped) looks. In the sequel we refer to this multi-look technique as the traditional technique.

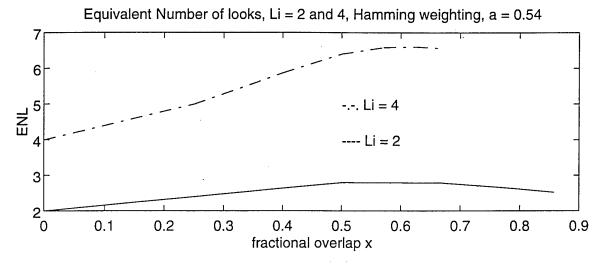


Figure 7: The ENL as a function of the fractional overlap.

#### 3.3 Hamming weighting function, two types of looks

The sections 3.1.3 and 3.2.2 are concerned with overlapping looks, 3.1.3 with looks computed with rectangular weighting functions and 3.2.2 computed with Hamming weighting functions. In both cases an ENL value is obtained larger than the number of independent looks. As explained this originates from the small values of the correlation coefficient values when the overlap is not too large. Since in the Hamming case an inefficient use of the signal spectrum is made by the independent looks, a large number of looks can be inserted with comparably small ρ-values. The 'holes' between the independent looks can profitably be filled with low ρ-value looks. However, the bandwidth at the extremities of the available bandwidth are still not well covered. In reference [1] this is remedied by a technique called the Improved Multi-Look technique (IML-technique). The extreme bandwidth is covered by smaller looks. The time interval length of a small look is the half of the length of a large one. Figure 8 shows how the looks are positioned in the spectral interval. In the next section, we derive the increased ENL and the decreased geometrical resolution.

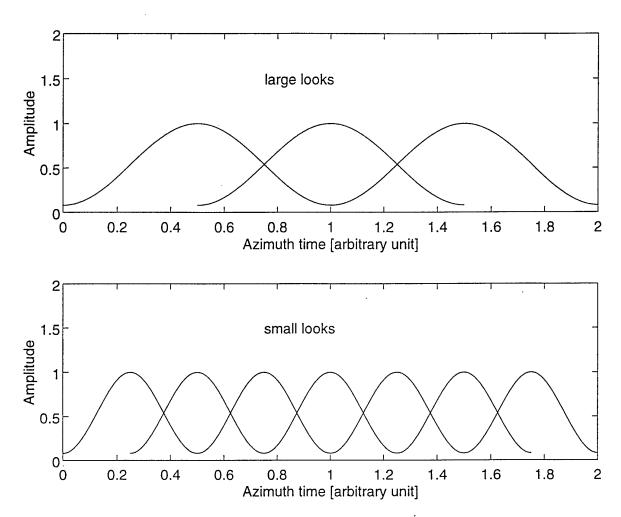


Figure 8: Look configuration of the IML technique,  $L_i = 2$ , overlap = 50%.

#### 3.3.1 L<sub>L</sub> overlapping large looks and L<sub>S</sub> overlapping small looks

The mean values and the (cross-)variances of the look images are given by

$$ar{I}_{L_i} = ar{I}_L$$
 for  $i = 1, 2, \dots, L_L$  
$$ar{I}_{s_j} = ar{I}_S = ar{I}_L/2$$
 for  $j = 1, 2, \dots, L_S$ 

The (cross-)variances are

$$\begin{split} &\overline{\left(I_{L_{i}} - \overline{I}_{L_{i}}\right)}\left(I_{L_{j}} - \overline{I}_{L_{j}}\right) = \rho_{I_{L_{i}}I_{L_{j}}}\sigma_{I_{L_{i}}}\sigma_{I_{L_{j}}} = \rho_{I_{L_{i}}I_{L_{j}}} \text{ var}(I_{L}) \\ &\overline{\left(I_{L_{i}} - \overline{I}_{L_{i}}\right)}\left(I_{S_{j}} - \overline{I}_{S_{j}}\right) = \rho_{I_{L_{i}}I_{S_{j}}}\sigma_{I_{L_{i}}}\sigma_{I_{S_{j}}} = \rho_{I_{L_{i}}I_{S_{j}}}\sigma_{I_{L}} \frac{\sigma_{I_{L}}}{2} = \rho_{I_{L_{i}}I_{L_{j}}} \frac{\text{var}}{2}(I_{L}) \\ &\overline{\left(I_{S_{i}} - \overline{I}_{S_{i}}\right)}\left(I_{S_{j}} - \overline{I}_{S_{j}}\right) = \rho_{I_{S_{i}}I_{S_{j}}}\sigma_{I_{S_{i}}}\sigma_{I_{S_{j}}} = \rho_{I_{S_{i}}I_{S_{j}}} \frac{\text{var}(I_{L})}{4} \end{split}$$

The multi-look intensity image is

$$I_M = \alpha_L \sum_{i=1}^{L_L} I_{L_i} + \alpha_S \sum_{j=1}^{L_S} I_{Sj}$$

Thus, the mean value

$$\overline{I}_{M} = \overline{\alpha_{L}} \sum_{i=1}^{L_{L}} I_{L_{i}} + \alpha_{S} \sum_{j=1}^{L_{S}} \ I_{Sj} = \alpha_{L} \sum_{i=1}^{L_{L}} \overline{I}_{L_{i}} + \alpha_{S} \sum_{j=1}^{L_{S}} \overline{I}_{Sj} = \alpha_{L} L_{L} \overline{I}_{L} + \alpha_{S} L_{S} \frac{\overline{I}_{L}}{2}$$

This mean value is chosen equal to the mean value of a large look. Thus

$$\alpha_L L_L \overline{I}_L + \alpha_S L_S \frac{\overline{I}_L}{2} = \overline{I}_L$$

Hence

$$\alpha_L L_L + \frac{\alpha_S L_S}{2} = 1$$

The variance is obtained by

$$var(I_{M}) = \overline{\left(I_{M} - \overline{I}_{M}\right)^{2}} = \overline{\left\{\alpha_{L}\sum_{i=1}^{L_{L}} \left(I_{L_{i}} - \overline{I}_{L_{i}}\right) + \alpha_{S}\sum_{j=1}^{L_{S}} \left(I_{Sj} - \overline{I}_{Sj}\right)\right\}^{2}}$$

$$= \alpha_{L}^{2}\sum_{i=1}^{L_{L}}\sum_{j=1}^{L_{L}} \sigma_{I_{L_{i}}} \sigma_{I_{L_{i}}} \rho_{I_{L_{i}}I_{L_{j}}} + 2\alpha_{L}\alpha_{S}\sum_{i=1}^{L_{L}}\sum_{j=1}^{L_{S}} \sigma_{I_{L_{i}}} \sigma_{I_{S_{j}}} \rho_{I_{L_{i}}I_{S_{j}}} + \alpha_{S}^{2}\sum_{i=1}^{L_{S}}\sum_{j=1}^{L_{S}} \sigma_{I_{S_{i}}} \sigma_{I_{S_{i}}} \rho_{I_{S_{i}}I_{S_{j}}}$$

$$= var(I_{L}) \left[\alpha_{L}^{2}\sum_{i=1}^{L_{L}}\sum_{j=1}^{L_{L}} \rho_{I_{L_{i}}I_{L_{j}}} + \alpha_{L}\alpha_{S}\sum_{i=1}^{L_{L}}\sum_{j=1}^{L_{S}} \rho_{I_{L_{i}}I_{S_{j}}} + \frac{\alpha_{S}^{2}}{4}\sum_{i=1}^{L_{S}}\sum_{j=1}^{L_{S}} \rho_{I_{S_{i}}I_{S_{j}}}\right]$$

Hence

$$ENL = \frac{1}{\left[\alpha_{L}^{2} \sum_{i=1}^{L_{L}} \sum_{j=1}^{L_{L}} \rho_{I_{L_{i}}I_{L_{j}}} + \alpha_{L}\alpha_{S} \sum_{i=1}^{L_{L}} \sum_{j=1}^{L_{S}} \rho_{I_{L_{i}}I_{S_{j}}} + \frac{\alpha_{S}^{2}}{4} \sum_{i=1}^{L_{S}} \sum_{j=1}^{L_{S}} \rho_{I_{S_{i}}I_{S_{j}}}\right]}$$

The correlation factor  $\rho = |\rho_{xy}|$  between two looks is a function of the weighting functions, the look sizes and the overlap. If we use an overlapping of 50% for both the large and the small looks, seven values of  $\rho$  can occur (see figure 8).

- 1. the looks do not overlap,  $|\rho_{xy}| = 0$
- 2. the looks are equal and completely overlap  $\rho = 1$
- 3. the large looks are correlated,  $\rho_L$
- 4. the small looks are correlated,  $\rho_S$
- 5. the large look and the small one are weakly correlated  $\rho_{SL1}$  (see figure 8, second small look from the left and the second large look from the left)
- 6. the large look and the small one are correlated  $\rho_{SL2}$  (first small and large look)
- 7. the large look and the small one are strongly correlated  $\rho_{SL3}$  (second small look and the first large look from the left).

As explained in appendix A,  $\rho_{ij} = \rho_{I_i I_j} = |\rho_{x_i x_j}|^2$ 

Substituting these values we obtain

$$ENL = \frac{1}{\alpha_{L}^{2} \left[ L_{L} + 2(L_{L} - 1)\rho_{L}^{2} \right] + \alpha_{L}\alpha_{S} \left[ 2(L_{L} - 1)\rho_{SL1}^{2} + 2L_{L}\rho_{SL2}^{2} + L_{L}\rho_{SL3}^{2} \right] + \frac{\alpha_{S}^{2}}{4} \left[ L_{S} + 2(L_{S} - 1)\rho_{S}^{2} \right]}$$

Using the equations from appendix A to calculate the correlation coefficient, we obtain

$$\rho_S^{~2}=0.0547\,,\;\rho_L^{~2}=0.0547\,,\;\rho_{SL1}^{~2}=0.0062\,,\;\rho_{SL2}^{~2}=0.2693$$
 and  $\rho_{SL3}^{~2}=0.7746$ 

The number of overlapping looks, given the number of independent looks  $L_i$ , is given by

$$L_L = 2L_i - 1$$
  
$$L_S = 4L_i - 1$$

As an example we consider the case for  $L_i = 4$ .

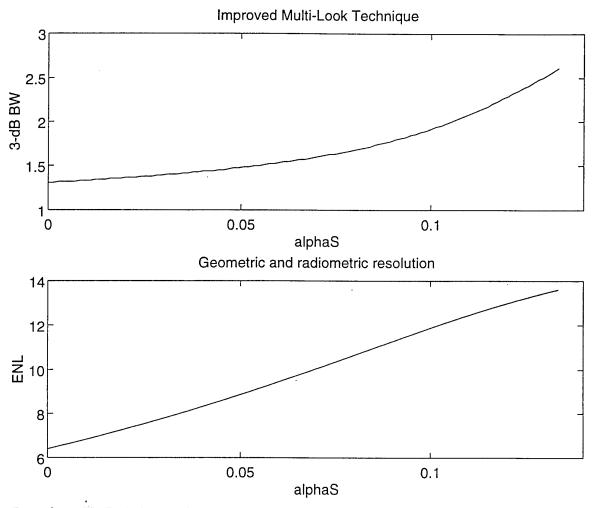


Figure 9: The Equivalent Number of Looks and the 3-dB resolution as a function of  $\alpha_S$ .

As shown by figure 9, increasing the value of  $\alpha_S$  leads indeed to an increase of the ENL and a decrease of the 3-dB BW.

However, this result is predictable as higher  $\alpha_S$  values correspond with an increasing relative contribution of the small looks, that is looks with a lower geometric resolution and we know that geometric resolution can be traded for radiometric resolution. For  $\alpha_S = 0$  we have the result of section 3.2.2 with  $L_i = 4$  (3-dB BW =1.30/Ba). For the other extreme  $\alpha_S$  value, corresponding to  $\alpha_L = 0$ , we have the result of section 3.2.2 with  $L_i = 8$  (3-dB BW = 2×1.30/Ba).

As a matter of fact, the technique offers to trade radiometric and geometric resolution in a continuous way via the parameter  $\alpha_S$ .

The technique fills the 'spectral dips' both in the middle part of the spectral range and at the extremities. The filling at the extremes sets this technique apart from other techniques. In order to prove the favourable effect of filling the edges, we compare the technique with one that fills the middle part in an optimum way. The latter technique uses looks each having the same size T (and Hamming weighting function). The available bandwidth is completely filled with L overlapping looks. The number of looks is taken such that the maximum ENL occurs. Both techniques yield the same geometrical resolution; this is done by choosing the corresponding values of  $\alpha_S$  and T. The comparison procedure is

- chose  $\alpha_S$  this yields the ENL<sub>IMI</sub> ( $\alpha_S$ ) and 3-dB BW ( $\alpha_S$ )
- take the corresponding 3-dB BW ( $\alpha_S$ ) value to determine the Hamming window size  $T(\alpha_S)$
- compute the optimum L value for this window, that is the value of L that yields the maximum ENL<sub>trad</sub>.

The results are shown in figure 10. From this figure we see that for almost all values  $\alpha_S$  the IML technique yields a higher ENL value. The exceptions are near the edges because there the techniques are equal (they use the same window size T), except for the overlap which is optimum for the traditional technique and 50% for the IML technique.

The quotient 
$$\frac{ENL_{IML}}{ENL_{trad}}$$
 reaches a maximum for  $\alpha_S = 0.08$ .

Figure 14 also shows that for the same geometrical resolution the IML technique performs better than the traditional.

Figures 11a and 11b show the azimuth impulse response of the IML technique for three values of  $\alpha_S$ . The value  $\alpha_S = 0$  yields the result of a single look image with  $L_i = 4$ . The other extreme value ( $\alpha_L = 0$ ) yields the results of a single look image with  $L_i = 8$ . The bottom curve shows the result for  $\alpha_S = 0.08$ . This result is especially interesting in that it shows the relative meaning of the geometric resolution measure in this case. Looking at the main lobe we see that only the upper part has the character of a lobe of a single look with the same 3-dB value. The bottom part corresponds with the lower geometrical resolution of the smaller look.

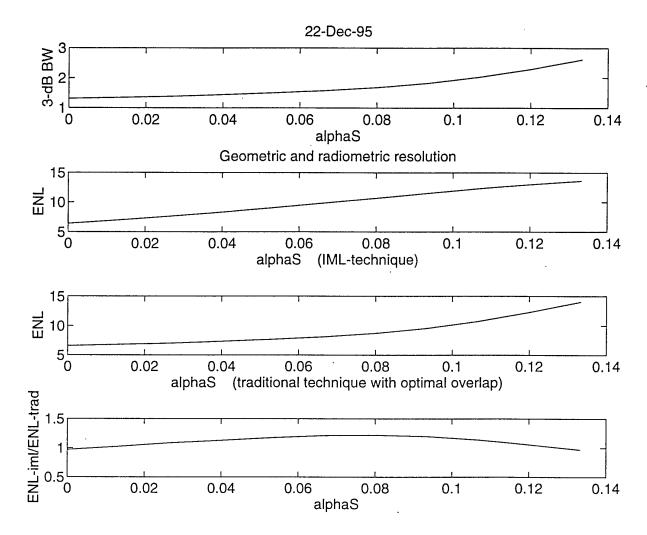


Figure 10: Comparison of the IML and traditional technique with optimum overlap.

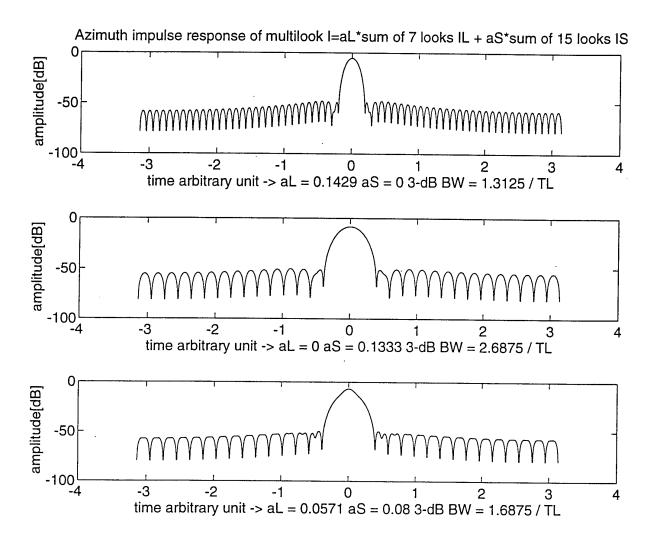


Figure 11a: Azimuth impulse response of the IML technique for several values of  $\alpha_S$ , logarithmic scale.

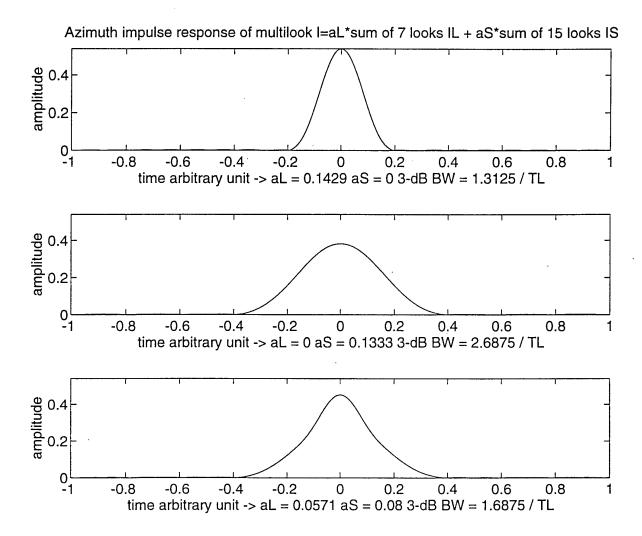


Figure 11b: Azimuth impulse response of the IML technique for several values of  $\alpha_S$ , linear scale.

#### 3.3.2 L<sub>L</sub> overlapping large looks and 2 small looks

Figure 12 shows the configuration of the technique. Comparing with figure 8 from the IML technique in section 3.3.1, we see that the small looks in the middle part of the available bandwidth are absent. The idea is that the radiometric resolution is improved by the two edge looks but that the geometrical resolution deteriorates less because of the small number of small looks.

The mean values and the (cross-)variances of the look images are given by

$$\overline{I}_{L_i} = \overline{I}_L$$
 for  $i = 1, 2, \dots, L_L$ 

$$\overline{I}_{S_j} = \overline{I}_S = \frac{I_L}{2}$$
 for  $j = 1, 2$ 

The cross variances are

$$\begin{split} \overline{\left(I_{L_{i}} - \overline{I}_{L_{i}}\right)} \left(I_{L_{j}} - \overline{I}_{L_{j}}\right) &= \rho_{I_{L_{i}}I_{L_{j}}} \sigma_{I_{L_{i}}} \sigma_{I_{L_{j}}} = \rho_{I_{L_{i}}I_{L_{j}}} \text{ var}(I_{L}) \\ \overline{\left(I_{L_{i}} - \overline{I}_{L_{i}}\right)} \left(I_{S_{j}} - \overline{I}_{S_{j}}\right) &= \rho_{I_{L_{i}}I_{S_{j}}} \sigma_{I_{L_{i}}} \sigma_{I_{S_{j}}} = \rho_{I_{L_{i}}I_{S_{j}}} \sigma_{I_{L}} \frac{\sigma_{I_{L}}}{2} = \rho_{I_{L_{i}}I_{S_{j}}} \frac{\text{var}(I_{L})}{2} \\ \overline{\left(I_{S_{i}} - \overline{I}_{S_{i}}\right)} \left(I_{S_{j}} - \overline{I}_{S_{j}}\right) &= 0 \text{ for } i \neq j \\ &= \sigma_{I_{S_{i}}} \sigma_{I_{S_{j}}} = \frac{\sigma_{I_{L}}^{2}}{4} = \text{var}(I_{L}) \text{ for } i = j \end{split}$$

Proceeding as in section 3.3.1 we arrive at

$$\bar{I}_{M} = \bar{I}_{L}$$

$$\alpha_L L_L + \frac{\alpha_S L_S}{2} = 1$$

and

$$ENL = \frac{1}{\alpha_L^2 \sum_{i=1}^{L_L} \sum_{i=1}^{L_L} \rho_{I_{L_i} I_{L_j}} + \alpha_L \alpha_S \sum_{i=1}^{L_L} \sum_{i=1}^{L_L} \rho_{I_{L_i} I_{S_j}} + \frac{\alpha_S^2}{4} \sum_{i=1}^{L_S} \sum_{i=1}^{L_S} \rho_{I_{S_i} I_{S_j}}}$$

As an example we consider the case for overlap = 50%, number of independent looks  $L_i = 4$ ,  $L_L = 2L_i-1$ ,  $L_S = 2$ .

Figure 13 shows the ENL and 3-dB BW as a function of  $\alpha_S$ , compare this figure with figure 9. Figure 14 shows the ENL as a function of the 3-dB BW; also shown are the curves of the traditional and IML technique.

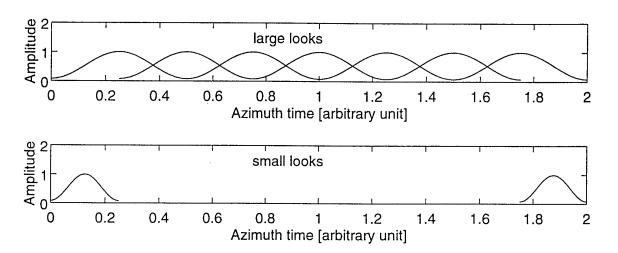


Figure 12: Look configuration of the technique,  $L_i = 4,50\%$  overlap.

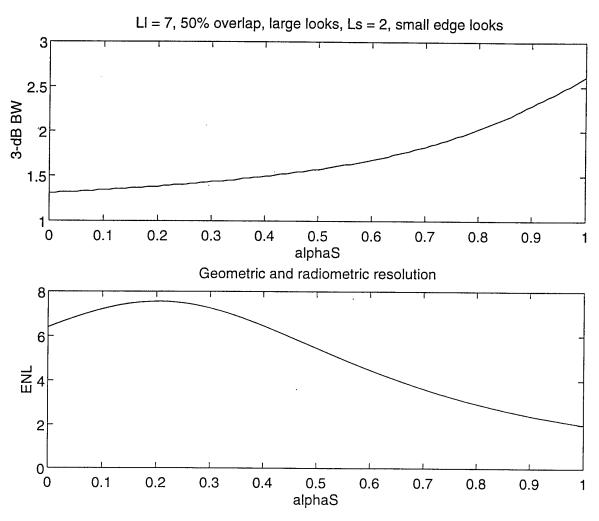
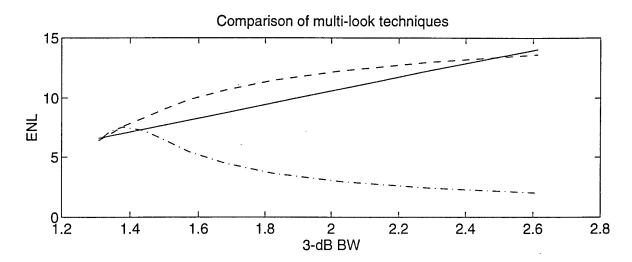


Figure 13: The Equivalent Number of Looks and the 3-dB resolution as a function of  $\alpha_S$ .

From this figure it can be concluded that this multi-look technique is not appreciably better than the IML technique. Only for the lower values it is slightly better and for the most part it is unusable. Note that in the 3-dB BW range, where it performs almost equally well as the IML technique, it does so in a far more efficient way, only 9 looks have to be computed compared with 22 in the IML case.

Figures 15a and 15b show the azimuth impulse response of the technique for three values of  $\alpha_S$ . The value  $\alpha_S = 0$  yields the result of a single look image with  $T = T_a/4$ . The other extreme value ( $\alpha_L = 0$ ) yields the result of a single look image with  $T = T_a/8$ . The bottom curve shows the result for  $\alpha_S = 0.2$  which corresponds with the maximum ENL value attainable. This curve shows, as its corresponding IML curve in figures 11a/b, the relative meaning of the geometric resolution measure in this case. Observing the main lobe, we see that only the upper part has the character of a lobe of a single look with the same 3-dB BW value. The bottom part corresponds with the lower geometrical resolution of the smaller look.



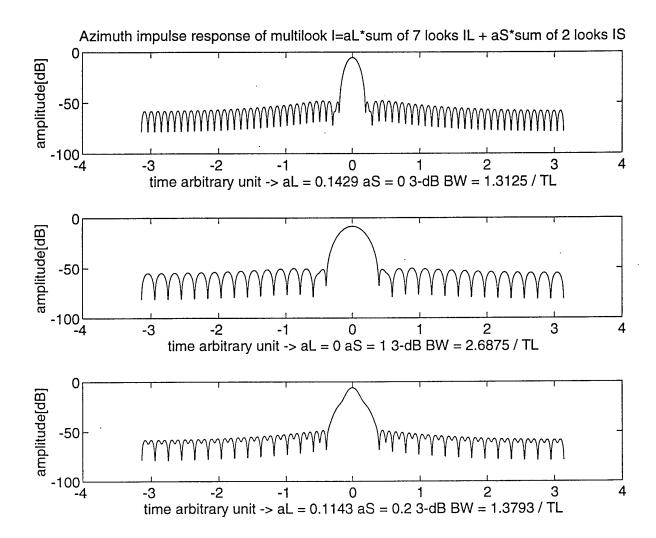


Figure 15a: Azimuth impulse response of the L7S2 multi-look technique for several values of  $\alpha_S$ , logarithmic scale.

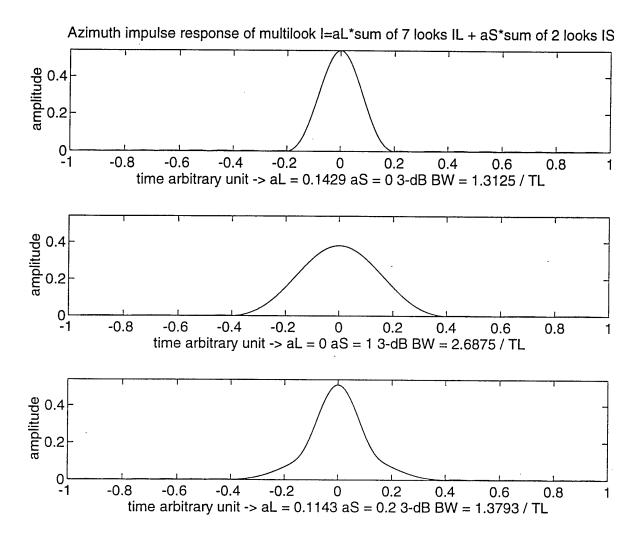


Figure 15b: Azimuth impulse response of the L7S2 multi-look technique for several values of  $\alpha_S$ , linear scale.

## 3.4 Two types of looks, different in weighting function and look size

#### 3.4.1 L<sub>L</sub> overlapping large looks and L<sub>S</sub> overlapping small looks

We proceed along the same lines as in section 3.3.1. The only difference being the mean value intensity of the small look. In 3.3.1 we considered the case where both weighting functions are Hamming ones and the look size of the small look is one half of that of the large look, thus  $\bar{I}_S = \bar{I}_L/2$ . In the general case the number 2 has to be replaced by another number, here called  $\beta_m$ , the value we derive below. The mean intensity value is

$$\overline{I} = P_c \int_{-T/2}^{T/2} w^2(t) dt$$

where

P<sub>c</sub> is the clutter power spectral density w(t) is the weighting function and T is the length of the weighting function.

Evaluating the mean values give

$$\bar{I}_R = P_c T_R$$
 and  $\bar{I}_H = 0.375 P_c T_H$ 

for the rectangular and Hamming windows respectively.

$$\beta_m = \frac{\overline{I}_L}{\overline{I}_S} = \frac{\overline{I}_H}{\overline{I}_R} = 0.3974 \frac{T_H}{T_R}$$

For the resolution holds

$$B_R = \frac{k_R}{T_R}$$
 and  $B_H = \frac{k_H}{T_H}$ 

with 
$$\frac{k_R}{k_H} = \frac{0.89}{1.30}$$
, see ref [3] table I.

Requiring equal resolution,  $B_R = B_H$ , we find  $T_R = \frac{k_R}{k_H} T_H = 0.685 T_H$  and  $\beta_m = 0.581$ .

The mean values and the (cross-)variances of the look images are given by

$$\bar{I}_{L_i} = \bar{I}_L$$
 for  $i = 1, 2, \dots, L_L$ 

$$\bar{I}_{s_i} = \bar{I}_S = \bar{I}_L / \beta_m$$
 for  $j = 1, 2, \dots, L_S$ 

The (cross-)variances are

$$\overline{\left(I_{L_{i}} - \overline{I}_{L_{i}}\right)\left(I_{L_{j}} - \overline{I}_{L_{j}}\right)} = \rho_{I_{L_{i}}I_{L_{j}}}\sigma_{I_{L_{i}}}\sigma_{I_{L_{j}}} = \rho_{I_{L_{i}}I_{L_{j}}} \text{ var}(I_{L})$$

$$\overline{\left(I_{L_{i}}-\bar{I}_{L_{i}}\right)\!\!\left(I_{S_{j}}-\bar{I}_{S_{j}}\right)}\!=\!\rho_{I_{L_{i}}I_{S_{j}}}\sigma_{I_{L_{i}}}\sigma_{I_{S_{j}}}=\rho_{I_{L_{i}}I_{S_{j}}}\sigma_{I_{L}}\frac{\sigma_{I_{L}}}{\beta_{m}}\!=\!\rho_{I_{L_{i}}I_{L_{j}}}\frac{var}{\beta_{m}}\!\!\left(I_{L}\right)$$

$$\overline{\left(I_{S_i} - \overline{I}_{S_i}\right)\!\!\left(I_{S_j} - \overline{I}_{S_j}\right)} \! = \! \rho_{I_{S_i}I_{S_j}} \sigma_{I_{S_i}} \sigma_{I_{S_j}} = \! \rho_{I_{S_i}I_{S_j}} \, \frac{var\!\left(I_L\right)}{\beta_m^2}$$

The multi-look intensity image is

$$I_{M} = \alpha_{L} \sum_{i=1}^{L_{L}} I_{L_{i}} + \alpha_{S} \sum_{j=1}^{L_{S}} I_{Sj}$$

Thus, the mean value

$$\overline{I}_{M} = \alpha_{L} \sum_{i=1}^{L_{L}} I_{L_{i}} + \alpha_{S} \sum_{j=1}^{L_{S}} I_{Sj} = \alpha_{L} \sum_{i=1}^{L_{L}} \overline{I}_{L_{i}} + \alpha_{S} \sum_{j=1}^{L_{S}} \overline{I}_{Sj} = \alpha_{L} L_{L} \overline{I}_{L} + \alpha_{S} L_{S} \frac{\overline{I}_{L}}{\beta_{m}}$$

This mean value is chosen equal to the mean value of a large look. Thus

$$\alpha_L L_L \bar{I}_L + \alpha_S L_S \frac{\bar{I}_L}{\beta_m} = \bar{I}_L$$

Hence

$$\alpha_L L_L + \frac{\alpha_S L_S}{\beta_m} = 1$$

The variance is obtained by

$$\begin{aligned} \text{var}(I_{M}) &= \overline{\left(I_{M} - \overline{I}_{M}\right)^{2}} = \overline{\left\{\alpha_{L} \sum_{i=1}^{L_{L}} \left(I_{L_{i}} - \overline{I}_{L_{i}}\right) + \alpha_{S} \sum_{j=1}^{L_{S}} \left(I_{Sj} - \overline{I}_{Sj}\right)\right\}^{2}} \\ &= \alpha_{L}^{2} \sum_{i=1}^{L_{L}} \sum_{j=1}^{L_{L}} \sigma_{I_{L_{i}}} \sigma_{I_{L_{j}}} \rho_{I_{L_{i}}I_{L_{j}}} + 2\alpha_{L} \alpha_{S} \sum_{i=1}^{L_{L}} \sum_{j=1}^{L_{S}} \sigma_{I_{L_{i}}} \sigma_{I_{S_{j}}} \rho_{I_{L_{i}}I_{S_{j}}} + \alpha_{S}^{2} \sum_{i=1}^{L_{S}} \sum_{j=1}^{L_{S}} \sigma_{I_{S_{i}}} \sigma_{I_{S_{j}}} \rho_{I_{S_{i}}I_{S_{j}}} \\ &= \text{var}(I_{L}) \left[\alpha_{L}^{2} \sum_{i=1}^{L_{L}} \sum_{i=1}^{L_{L}} \rho_{I_{L_{i}}I_{L_{j}}} + \frac{2}{\beta_{m}} \alpha_{L} \alpha_{S} \sum_{i=1}^{L_{L}} \sum_{j=1}^{L_{S}} \rho_{I_{L_{i}}I_{S_{j}}} + \frac{\alpha_{S}^{2}}{\beta_{m}^{2}} \sum_{i=1}^{L_{S}} \sum_{j=1}^{L_{S}} \rho_{I_{S_{i}}I_{S_{j}}} \right] \end{aligned}$$

Hence

$$ENL = \frac{1}{\left[\alpha_{L}^{2} \sum_{i=1}^{L_{L}} \sum_{j=1}^{L_{L}} \rho_{I_{L_{i}} I_{L_{j}}} + \frac{2}{\beta_{m}} \alpha_{L} \alpha_{S} \sum_{i=1}^{L_{L}} \sum_{j=1}^{L_{S}} \rho_{I_{L_{i}} I_{S_{j}}} + \frac{\alpha_{S}^{2}}{\beta_{m}^{2}} \sum_{i=1}^{L_{S}} \sum_{j=1}^{L_{S}} \rho_{I_{S_{i}} I_{S_{j}}}\right]}$$

#### 3.4.2 L<sub>L</sub> overlapping large Hamming looks and 2 small rectangular looks

Figure 16 shows the positions of the various looks associated with this technique, referred to as the HL7RS2 technique. Comparing with figure 12 in section 3.3.2 we see that the small Hamming weighted looks are replaced by small rectangular ones. The expectation is that by using rectangular weighting functions for the extreme looks rather than Hamming weighted ones we are able to improve the radiometric resolution via the edge looks without having to sacrifice geometrical resolution.

In section 3.3.2 we used edge looks with half the look size of the large ones. The resolution of a rectangular look with this look size is better than the Hamming look resolution but still worse than the resolution associated with the large Hamming look. To obtain the same geometrical resolution we have to use a larger rectangular look size. Below we consider two cases: one case where the resolution of an edge look equals that of a large Hamming look and one where the look size of the edge look is one half of that of a large look.

Note that by choosing the 3 dB resolution of the rectangular edge look equal to the resolution of the large Hamming look the sidelobe performance of the former is worse.

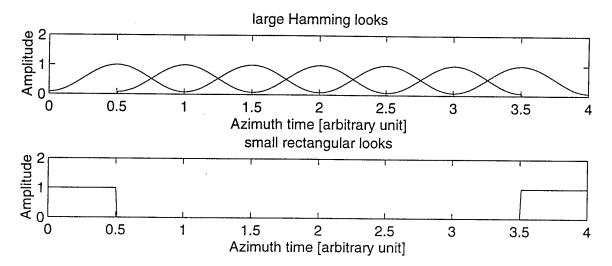


Figure 16: Look configuration of the HL7RS2 multi-look technique.

As derived in section 3.4.1 we have

$$\bar{I}_m = \bar{I}_L$$

$$\alpha_L L_L + \frac{\alpha_S L_S}{\beta_m} = 1$$

$$ENL = \frac{1}{\alpha_L^2 \sum_{i=1}^{L_L} \sum_{j=1}^{L_L} \rho_{I_{L_i} I_{L_j}} + \frac{2}{\beta_m} \alpha_L \alpha_S \sum_{i=1}^{L_L} \sum_{j=1}^{L_S} \rho_{I_{L_i} I_{S_j}} + \frac{\alpha_S^2}{\beta_m^2} \sum_{i=1}^{L_S} \sum_{j=1}^{L_S} \rho_{I_{S_i} I_{S_j}}}$$

and

$$\beta_{m}=0.3974\frac{T_{H}}{T_{R}}$$

As an example, we take an overlap of 50% for the large Hamming windows, the number of independent looks  $L_i = 4$ ,  $L_L = 2L_{i-1}$  and  $L_S = 2$ .

The figures 17 through 18a,b show the results where the resolution of the rectangular edge look is equal to the resolution of the large Hamming look. As derived in section 3.4.1 then  $T_R = 0.685 \, T_H$  and  $\beta_m = 0.581$ .

Figure 17 shows the ENL and 3 dB values as a function of  $\alpha_S$ . The maximum ENL value occurs for  $\alpha_S = 0.0351$  and is equal to 6.70. This value is less than 7.6, the value obtained with Hamming edge looks. However, in the latter case the resolution is less, 1.38 compared to 1.31. Compared to the IML technique we notice that the HL7RS2 technique offers a

slight advantage in the low  $\alpha_S$  range. The ENL values are almost equal but no

resolution is sacrificed. Also, the efficiency is higher, only 9 looks have to be computed compared with 22 in the IML case.

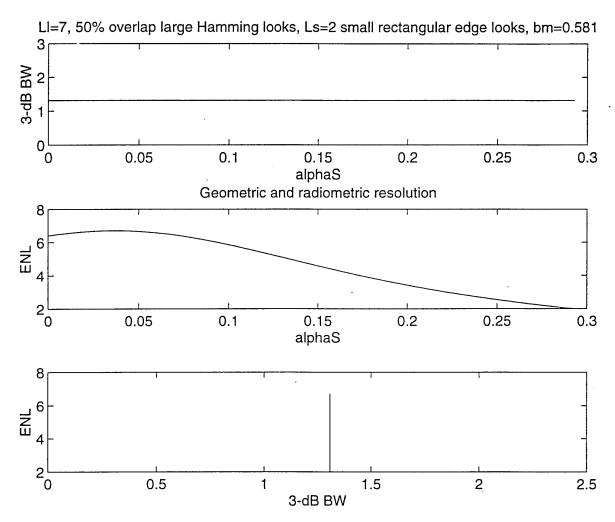


Figure 17: The Equivalent Number of Looks and the 3 dB resolution as a function of  $\alpha_S$ . All looks same resolution,  $\beta_m = 0.581$ .

Figures 18a and b show the azimuth impulse response of the HL7RS2 technique for three values of  $\alpha_S$ . The value  $\alpha_S = 0$  yields the result of a single look Hamming weighted image with  $T_H = T_a/4$ . The other extreme value ( $\alpha_L = 0$ ) yields the result of a single look rectangular weighted image with  $T_R = 0.685T_a/4$ . The bottom curve shows the result for  $\alpha_S = 0.0351$  which corresponds with the maximum ENL value attainable. Note that although the 3 dB resolution is equal to the resolution of the all Hamming case, the sidelobe character is worse due to the higher sidelobes of the rectangular look.

Figure 19 shows the result obtained with the HL7RS2 technique for  $T_R = T_H/2$ ,  $\beta_m = 0.795$ . This figure can be compared with Figure 13, results from the HL7HS2 technique. In both figures we observe the  $\alpha_S$  dependence of the resolution due to the inequality of the resolution of small and large looks. The HL7RS2 technique yields a maximum ENL value of 7.52 for  $\alpha_S = 1.356$ . The values for the HL7HS2

technique are ENL = 7.56 for  $\alpha_S$  = 0.2. Thus the HL7RS2 technique yields a slightly smaller ENL value. However, the resolution is better, 3 dB value is 1.36 compared with 1.38, the HL7HS2 value.

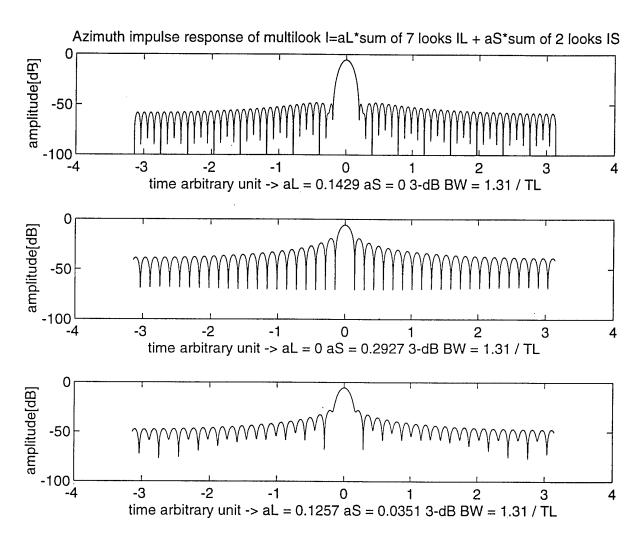


Figure 18a: Azimuth impulse response of the HL7RS2 multi-look technique for several values of  $\alpha_S$ , logarithmic scale.

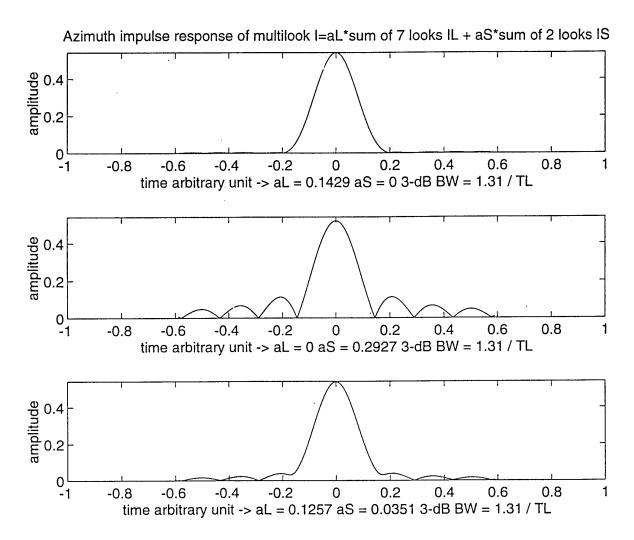


Figure 18b: Azimuth impulse response of the HL7RS2 multi-look technique for several values of  $\alpha_S$ , linear scale.

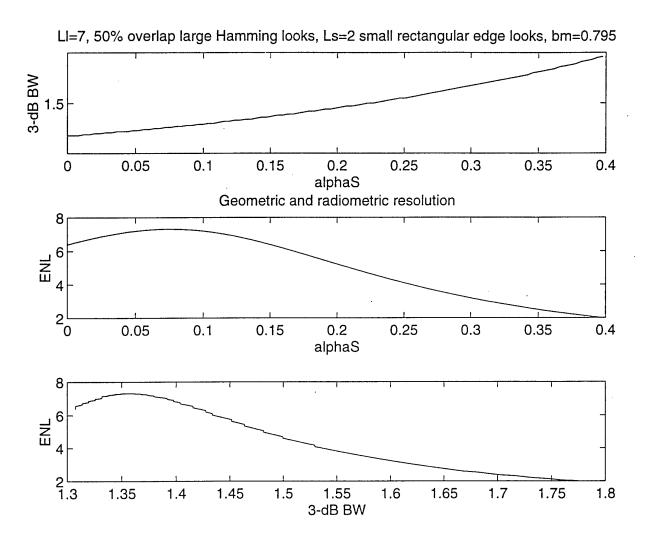


Figure 19: The Equivalent Number of Looks and the 3 dB resolution as a function of  $\alpha_S$ .  $T_R = T_H/2$ ,  $\beta_m = 0.795$ .

#### 3.5 Visual illustrations of multi-look techniques

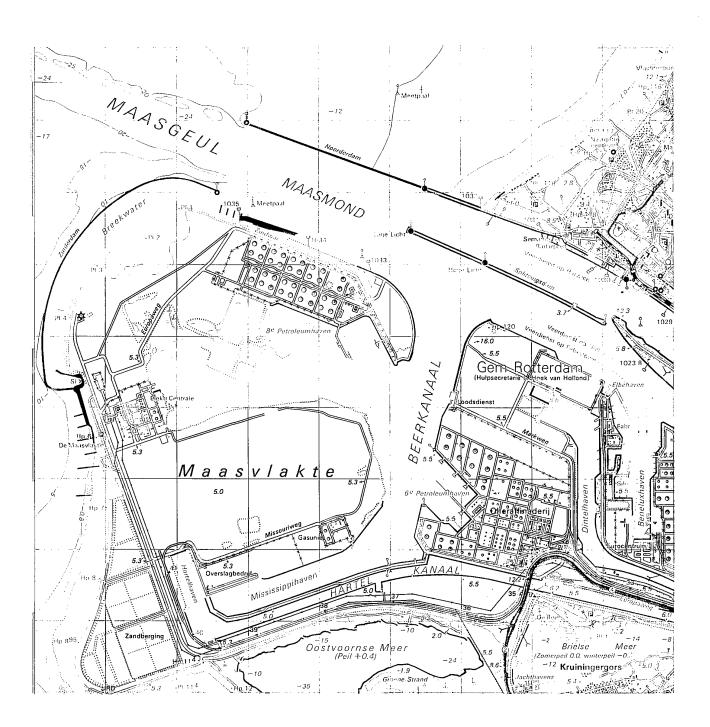
The results of various multi-look techniques are shown in the form of the images R2, R3 and R4. The techniques have been implemented in the Generic SAR Processor (GSP) of TNO-FEL. The GSP is a software package that runs on a SUN workstation and is able to process both airborne and satellite SAR data. The raw SAR input data is part of raw image data of the ERS1 satellite SAR. The scene consists of the entrance to the port of Rotterdam and part of its environment. A map of the area is shown by R1.

Output of the processor are 7 single-look images (L0, L1, L2, L3, L4, L5 and L6). The images have 50% overlap. Hamming weighting is used. The slant range resolution is 9 m and the azimuth resolution is 32 m.

Image R2 shows the central single-look image L3. The speckle noise is clearly visible, masking weak details and interrupting line structures. The interruption occurs as a low speckle value is realised.

Image R3 shows the multi-look image consisting of the combination of the 4 non overlapping looks: L0, L2, L4 and L6. The corresponding equivalent number of looks ENL = 4. The speckle reduction, compared to R2, is clearly visible, more weak details emerge and very few line structures are interrupted. The probability of occurrence of a low speckle value in each of the four images is low. Image R4 shows the multi-look image consisting of the combination of all 7 single-look images, L0 through L6. The corresponding equivalent number of looks is ENL = 6.4. Again an improvement can be observed albeit less than going from R2 to R3.

Some remarks are in order. First, visual quality is higher on a monitor, some is lost by the copying process. Second, speckle reduction is advantageous to both men and machine. A human interpretor sees more weak details. A computer algorithm can use the improved signal-to-noise ratio to perform better. Degrees of speckle reduction insignificant to man can still be useful for very demanding applications.



R1: Map of the environment of the entrance to the port of Rotterdam.



Single look of L4 independent looks.



Multi-look image, combination of 4 independent looks.



Multi-look image, combination of 7 overlapping looks.

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### 4. The azimuth impulse response

In order to assess a multi-look technique two values are important: the Equivalent Number of Looks (ENL) and the resolution measured by the 3 dB width of the main lobe (BW) of the azimuth impulse response. The impulse response of the multi-look technique is a weighted sum of the responses of the large and small looks.

$$I_{M} = \alpha_{L} \sum_{i=1}^{L_{L}} I_{L_{i}} + \alpha_{S} \sum_{j=1}^{L_{S}} I_{S_{j}}$$

The main lobe width BW is determined via an iterative procedure. For an accurate result a densely sampled impulse response  $I_M$  is required. If the constituent response sequences  $I_L$  and  $I_S$  are given in formula form, the samples are readily computed. In this report only the rectangular and Hamming weighting functions are considered and the corresponding response functions are analytically known, at least the main lobe part. So, we have used the known formulae. If these formulae were not known, a numerically obtained response sequence must be used. In this case the sequence must be heavily interpolated to yield a result which can be used for a sufficiently accurate BW value.

In the report a number of azimuth impulse responses are shown. The main lobe of these curves were used to determine the BW value. Use of the analytical description of the main lobe is correct, however, the description is not correct for the sidelobes [ref. 5, section 7.6]. The derived formulae are based on the assumption that the linear FM spectrum has a rectangular amplitude distribution. The amplitude ripple of the actual spectrum can be related to the existence of distortion sidelobes that can be considerably greater than the -40 dB level that can be obtained by the Hamming weighting (see Figure 7.22 in ref. 5).

The Figures 20a and 20b show the azimuth impulse responses of the HL7HS2 multi-look technique. These curves were obtained by computer simulation (digitally computed cross correlation sequence). Comparing these figures with the ones shown by the figures 15a and b, which are based on the analytical description of the main lobe, we see a marked difference in sidelobe behaviour.

The computer simulated curves were obtained by using the ERS-1 satellite parameters. The full resolution azimuth response uses a bandwidth of  $Ba = 1300 \ Hz$  and an integration time of  $T_a = 0.6 \ sec$ , yielding a bandwidth time product of about 800.

The spectrum corresponding to such a high BT product shows fairly well a rectangular amplitude distribution and a very good sidelobe behaviour (not shown here). However, the large and small looks have BT products which are much lower. For instance, the small look spans Ta/8 seconds. The azimuth frequency rate is  $\frac{B_a}{T_a}$  thus, the look has a BT product of only  $\frac{T_a}{8} \cdot \frac{B_a}{T_a} \cdot \frac{T_a}{8} = \frac{B_a T_a}{64} = 12.5$ 

Therefore, the spectrum is far from rectangular and a decreased sidelobe character can be expected.

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Thus, we conclude that the shown azimuth impulse responses must be interpreted with care, the main lobe part is correct, however, the sidelobe behaviour is too optimistic.

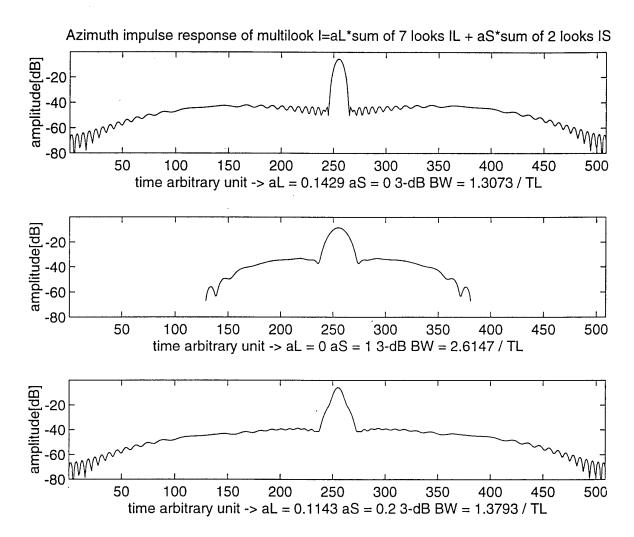


Figure 20a: Azimuth impulse response of the HL7RS2 multi-look technique for several values of  $\alpha_S$ , logarithmic scale.

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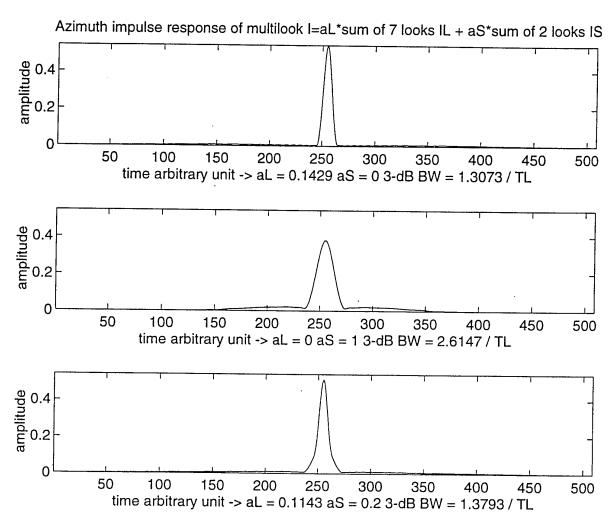


Figure 20b: Azimuth impulse response of the HL7RS2 multi-look technique for several values of  $\alpha_S$ , linear scale.

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### 5. Conclusions

We have evaluated the effects on SAR imagery of a number of different speckle reduction techniques. Each technique uses a number of single look intensity images of which the weighted sum, the multi-look image is formed. The constituent single looks differ in size T (B) and weighting function used. It is shown that the speckle behaviour of each look is the same and that they differ in geometric resolution, i.e. the width of the main lobe of the impulse response. Since, the lower geometric resolution looks do not make efficient use of the signal energy, speckle reduction can be obtained, increase in the ENL's, by multi-look technique. By using overlapping looks, a more efficient use is made of the available bandwidth.

We have evaluated three types of techniques: techniques using equal looks with a rectangular weighting function, techniques that use equal looks with a Hamming weighting function, and techniques that use two kinds of weighting function sizes. It has been shown that the last techniques are able to fill the left and right extremities of the signal bandwidth by positioning there small looks. However, the general pattern, trading geometric resolution for radiometric resolution, holds, since the smaller looks have a lower geometric resolution. The IML technique forms the multi-look image by computing the weighted sum of the large and small looks. By varying the factor  $\alpha_S$  continuously a continuous trading of geometric and radiometric resolution is obtained.

As a measure of geometric resolution, the 3-dB width of the main lobe of the impulse response is used. However, two responses can have the same 3-dB value and differ in detailed main lobe and sidelobe structures. The effects of different impulse response shapes on image interpretation may be important. We have analysed the techniques assuming a flat azimuth spectrum. The effects of the shape of the spectrum can be analysed for each individual system and a more realistic value of the ENL can be calculated. A potential drawback of the multilook techniques yielding improved ENL values is that many more looks have to be computed. However, there may be cases where the utmost attainable ENL value is a necessity.

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#### Signature 7.

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Author

## Appendix A The correlation coefficients $\rho_{xy}$ and $\rho_{I_xI_y}$

# A.1 The correlation coefficient $\rho_{XY}$ of two complex valued single look images

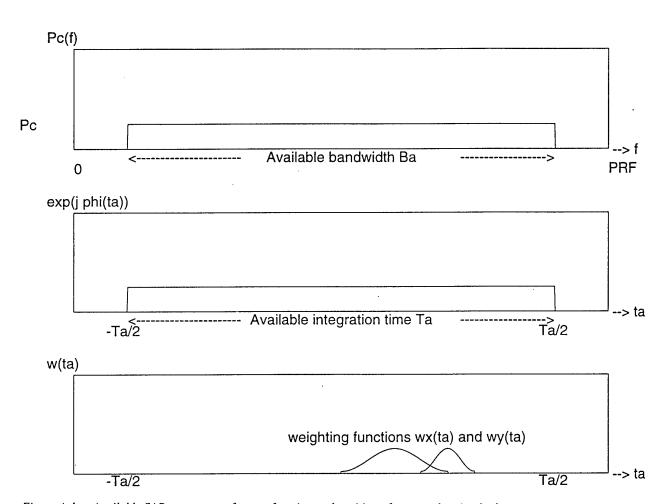


Figure A.1: Available SAR spectrum, reference function and position of two overlapping looks.

The cross spectral density of two complex single look images is

$$P_{xy}(f) = H_x(f)H_y^*(f)P_c(f)$$

where  $H_x(f)$  and  $H_y(f)$  are the frequency transfer functions of the x and y outputs respectively, and  $P_c(f)$  is the azimuth clutter power density spectrum.

The cross-covariance  $\mu_{xy} = (x - \overline{x})(y - \overline{y})^*$  is given by

$$\mu_{xy} = R_{xy}(0) = \int P_{xy}(f) df = P_c \int H_x(f) H_y^*(f) df = P_c \int h_x(t) h_y^*(t) dt$$

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The azimuth reference function is

$$h(t) = \epsilon^{j\phi(t)} - T_a/2 \le t \le T_a/2$$

Hence the look reference functions are

$$h_x(t) = w_x(t - t_{c_x})h(t)$$
  $t_{c_x} - T_x/2 \le t \le t_{c_x} + T_x/2$ 

$$h_y(t) = w_y(t - t_{c_y})h(t)$$
  $t_{c_y} - T_y/2 \le t \le t_{c_y} + T_y/2$ 

where  $w_x(\ )$  and  $w_y(\ )$  are the (real) window functions. Substitution gives

$$\mu_{xy} = P_c \int w_x(t - t_{cx})h(t)w_y(t - t_{cy})h^*(t)dt$$

$$\mu_{xy} = P_c \int w_x (t - t_{cx}) w_y (t - t_{cy}) dt$$

Without loss of generality we take  $T_x \ge T_y$  and  $t_x = 0$ . Thus

$$\mu_{xy} = P_c \int w_x(t) w_y(t - t_{c_y}) dt$$

The variance of x and y are

$$\operatorname{var}(x) = \overline{(x-\overline{x})(x-\overline{x})^*} = P_c \int w_x^2(t) dt$$

$$var(y) = \overline{(y - \overline{y})(y - \overline{y})^*} = P_c \int w_y^2(t) dt$$

Hence, the correlation coefficient  $\rho_{xy} = \frac{\mu_{xy}}{\sigma_x \sigma_y}$  is

$$\rho_{xy} = \frac{\int w_x(t)w_y(t - t_{cy})dt}{\sqrt{\int w_x^2(t)dt}\sqrt{\int w_y^2(t)dt}}$$

### A.2 The correlation coefficient $\rho_{I_xI_y}$ of two intensity images

The statistics of the real and imaginary part of the complex valued images x and y are

$$\overline{x_r} = \overline{x_i} = 0$$

$$\overline{x_r x_i} = 0$$

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$$var(x_r) = var(x_i) = \sigma_x^2$$

$$\overline{y_r} = \overline{y_i} = 0$$

$$\overline{y_r y_i} = 0$$

$$var(y_r) = var(y_i) = \sigma_v^2$$

$$\overline{x_r y_r} = \overline{x_i y_i}$$

$$\overline{x_r y_i} = -\overline{x_i y_r}$$

The stochastic variables  $x_r$ ,  $x_i$ ,  $y_r$  and  $y_i$  have a Gaussian probability density function. Thus the intensity has an exponential pdf with

$$I_x = 2\sigma_x^2$$

$$var(I_x) = I_x^2 = 4\sigma_x^4$$

Thus, the statistics of the complex valued images are

$$\overline{x} = \overline{x_r + jx_i} = 0$$

$$var(x) = \overline{(x-x)(x-x)^*} = \overline{xx^*} = \overline{x_r^2} + \overline{x_i^2} = 2\sigma_x^2$$

$$\overline{y} = \overline{y_r + jy_i} = 0$$

$$var(y) = \overline{(y-\overline{y})(y-\overline{y})^*} = \overline{yy^*} = \overline{y_r^2} + \overline{y_i^2} = 2\sigma_v^2$$

$$\mu_{xy} = \overline{(x - \overline{x})(y - \overline{y})^*} = \overline{xy^*} = \overline{x_r y_r} + \overline{x_i y_i} + j(\overline{x_i y_r} - \overline{x_r y_i}) = 2(\overline{x_r y_r} + j \overline{x_i y_r})$$

The correlation coefficient between x and y is given by

$$\rho_{xy} = \frac{\mu_{xy}}{\sqrt{\text{var}(x)}\sqrt{\text{var}(y)}} = \frac{\overline{x_r y_r} + j \overline{x_i y_r}}{\sigma_x \sigma_y}$$

Hence

$$\left|\rho_{xy}\right|^2 = \frac{\overline{x_r y_r}^2 + \overline{x_i y_r}^2}{\sigma_x^2 \sigma_y^2}$$

The real valued intensity images are

$$I_x = x_r^2 + x_i^2$$

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$$I_v = y_r^2 + y_i^2$$

Thus, the statistics of the intensity images are

$$\overline{I}_x = \overline{x_r^2} + \overline{x_i^2} = 2\sigma_x^2$$

$$\overline{I}_y = \overline{y_r^2} + \overline{y_i^2} = 2\sigma_v^2$$

$$var(I_x) = \overline{(I_x - \overline{I}_x)^2} = 4\sigma_x^4$$

$$var(I_y) = \overline{(I_y - \overline{I}_y)^2} = 4\sigma_y^4$$

The cross-covariance is

$$\mu_{I_xI_y} = \overline{\left(I_x - \overline{I}_x\right)\!\!\left(I_y - \overline{I}_y\right)} = \overline{I_xI_y} - \overline{I}_x\,\overline{I}_y = \overline{I_xI_y} - 4\sigma_x^2\sigma_y^2$$

$$\overline{I_x}\overline{I}_y = \overline{\left(x_r^2 + x_i^2\right)\!\!\left(y_r^2 + y_i^2\right)} = \overline{x_r^2y_r^2} + \overline{x_r^2y_i^2} + \overline{x_i^2y_r^2} + \overline{x_i^2y_r^2}$$

Since x<sub>r</sub> and y<sub>r</sub> are Gaussian

$$\overline{x_r^2 y_r^2} = \overline{x_r^2 y_r^2} + 2 \overline{x_r y_r^2}$$

Substitution yields

$$\overline{I_x I_y} = 4 \left( \overline{x_r y_r}^2 + \overline{x_i y_r}^2 \right)$$

Thus

$$\rho_{I_xI_y} = \frac{\mu_{I_xI_y}}{\sqrt{var(I_x)\sqrt{var(Iy)}}} = \frac{\overline{x_ry_r}^2 + \overline{x_iy_r}^2}{\sigma_x^2\sigma_y^2}$$

Hence

$$\rho_{I_xI_y} = \left| \rho_{xy} \right|^2$$

The correlation coefficient of the intensity images is equal to the modules squared of the correlation coefficient of the complex images.

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discuss the performance of sev resolution of the impulse respo the use of single looks, number	eral techniques to generate onse can be traded for the ra c, size and weighting functi	ok imaging is used for its alleviation. In this report, we multi-look images. It is shown that the geometric adiometric resolution. The various techniques differ in on. It is found that by properly positioning of umber of looks is substantially higher than the
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